

# A Novel Method for Quantifying Arm Motion Similarity

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**Abstract**—This paper proposes a novel task-independent method for quantifying arm motion similarity that can be applied to any kinematic/dynamic variable of interest. Given two arm motions for the same task, not necessarily with the same completion time, it plots the time-normalized curves against one another and generates four real-valued features. To validate these features we apply them to quantify the relationship between healthy and paretic arm motions of chronic stroke patients. Studying both unimanual and bimanual arm motions of eight chronic stroke patients, we find that inter-arm coupling that tends to synchronize the motions of both arms in bimanual motions, has a stronger effect at task-relevant joints than at task-irrelevant joints. It also revealed that the paretic arm suppresses the shoulder flexion of the non-paretic arm, while the latter encourages the shoulder rotation of the former.

## I. INTRODUCTION

Bimanual arm motions are characterized by temporal and spatial coupling, due to which the arms tend to move symmetrically [1]–[3]. For stroke patients with motor disability (i.e., hemiparesis), inter-arm coupling tries to synchronize the paretic arm with the non-paretic arm despite of deteriorated motor function, which might aid recovery [4]. Studies of chronic stroke patients have shown that the peak velocities of the paretic arm were increased in symmetrical bilateral motions, at the expense of deteriorated performance of the non-paretic arm [5], [6]. Due to inter-arm coupling, the paretic arm may improve its motor function by moving with the non-paretic arm, which has been reported in a therapy with symmetrical exercises (e.g., Bobath neuro-developmental approach) and other bilateral training therapies [7]–[10].

The neural mechanisms of human motor control have been investigated (for comprehensive review see [11]). However, clinical studies still argue whether bilateral training is more effective than alternative therapies [12], [13], mostly due to the lack of a consistent measurement that can compare motor function recovery across therapies that differ in their tasks. Previous research efforts on the symmetry of bimanual motions compare arm motions either using the kinematic/dynamic variables of the two arms (e.g., motion timing, hand trajectory, muscle activity, etc.), or by various task-dependent performance indexes (e.g., the aspect ratio for circle drawing tasks) [14]–[21]. Due to differences in tasks,

these measurements of kinematic/dynamic variables cannot be directly compared across studies.

This paper proposes a method to quantify the motion similarity of two arms regardless of the task, which is generally applicable to any kinematic and dynamic variables of interest. The idea behind the method is to map two motions against one another, and quantify the similarity and complexity of the mappings via four real-valued feature variables. For both in-phase and anti-phase motions, the extracted feature variables can characterize the motion similarity of two arms, as well as of the same arm across trials. To validate the utility of these features, data was collected from chronic stroke patients on unimanual and bimanual motions of identical tasks. The features were applied to quantify mapping similarity between arms, and on the same arm in both the bimanual and unimanual conditions. The features are sufficiently sensitive to indicate the behavior changes of the non-paretic and paretic arms, and suggest that the effect of inter-arm coupling is stronger on the task-relevant joints than the task-irrelevant joints in symmetric arm motions.

## II. METHODOLOGY

### A. Quantification of Motion Similarity

The proposed method uses three mapping symmetry features and one mapping complexity feature to quantify the similarity of two motions. First, a kinematic/dynamic feature (e.g., joint angle) of one motion is plotted against the other motion with correspondences determined along a normalized time dimension. Fig. 1 shows the mapping of joint angles (denoted by  $\theta_i$  and  $\theta'_i$ ) between two motions. Next, linear regression is used to find the **the absolute value of the slope**  $p_1$  and the **intersection**  $p_2$  for the mapping (i.e.,  $\theta'_i = p_1\theta_i + p_2$ ). The coefficient of determination  $R^2$  is computed, referred as the **mapping linearity**. Note that  $p_1 \in [0, +\infty]$ ,  $p_2 \in [-\infty, +\infty]$ , and  $R^2 \in [0, 1]$ . For ideally symmetric motions, the mapping plots are straight line segments with  $p_1 = 1$ ,  $p_2 = 0$  and  $R^2 = 1$ . Larger deviations from these values indicate less motion similarity. The last feature measures **mapping complexity**  $N_c$ . Mappings of similar motions (in-phase or anti-phase) are well approximated by a single line, while more complex mappings would require multiple line segments to achieve tolerable accuracy. This feature measures how many line segments are needed for fitting the mapping with a pre-determined accuracy level.

Fig. 1a to 1c illustrate the significance of each mapping symmetry feature. For a mapping of two motions,  $p_1$  indicates which motion traverses more of the joint space. Different average postures between two motions result in a non-zero  $p_2$ , while nonlinear deviations make  $R^2 < 1$ .

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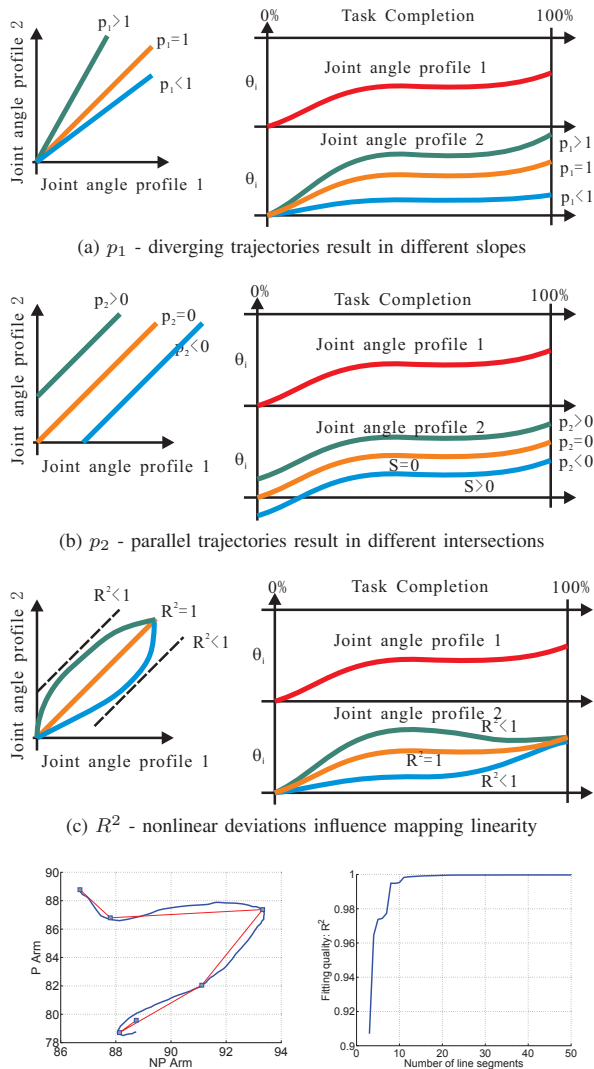


Fig. 1: The mapping symmetry and complexity features.

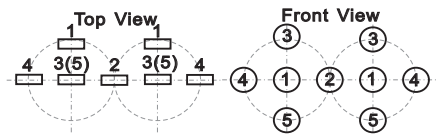
For inter-arm mappings, mapping symmetry features indicate motion differences between the arms. For mappings between unimanual and bimanual motions, these features measure arm behavior changes due to inter-arm coupling. In Fig. 1d, piecewise linear regression is applied to an inter-arm mapping for the elbow flexion  $\theta_4$  of a stroke patient. As the number of line segments necessary (denoted by  $N$ ) goes up, the fitting quality increases and eventually stabilizes (refer to Fig. 1d). To represent the shape of a mapping plot without over-fitting, the mapping complexity  $N_c$  is defined as the smallest  $N$  with coefficient of determination of the piecewise linear fitting larger than some threshold  $\alpha$  ( $\alpha$  was chosen to be 0.95 throughout this paper). The mapping complexity of two motions reflects the difficulty in generating one motion given the knowledge of the other. It is similar to the mapping linearity feature  $R^2$ , since the mismatching of two motions results in more turning points in the mapping plot and

thus more approximation segments, yet a mapping plot that consists of a few largely non-collinear segments may have large mapping linearity but low mapping complexity.

## B. Subjects, Protocol and Experimental Setups



(a)



(b)

Fig. 2: In reaching experiments, (a) passive reflective markers are attached to the arms and torso of the subjects for position tracking; (b) targets for each hand are aligned on circles centered on the subject's shoulders.

The data for this study were collected from eight chronic stroke patients, ranged in age from 53 to 72 years old (average  $60.4 \pm 7.2$ ). Among the eight subjects, six were impacted on the right arm and two on the left arm. Subjects scored between 20 and 27 on the upper limb volitional motion portions of the Fugel-Meyer assessment, out of a total score of 30. Fig. 2a depicts the workspace setup of the experiment. As shown in Fig. 2b, the left/right targets are arranged on the surfaces of spheres corresponding to the left/right hand of the subject. The center and radius of the two spheres are adjusted according to the shoulder width and height of the subject to align Target 1 in each sphere with the corresponding shoulder. The distance between the subject and the workspace is adjusted such that the subject can reach each target comfortably. During the experiment, the subject starts from resting their arms on the handle of the chair, with consistent wrist positions. At a “go” command, the subject starts reaching for the instructed target, touching the target with the tip of the tool held in hand. The experiment consists of two unimanual sessions and one bimanual session. In the unimanual sessions, the subjects reach with their left/right hand to the five targets corresponding to that hand. In the bimanual session, the subjects reach for both the left and right targets symmetrically. Each session consists of 25 individual trials (5 targets  $\times$  5 repetitions). A motion capture system records the trials at a sampling rate of 100 Hz. Subjects rest after each session to minimize fatigue. Based on the recorded shoulder, elbow and wrist positions (denoted by  $P_s$ ,  $P_e$  and  $P_w$  respectively), trajectories of the four joint angles were computed by inverse kinematics (see Fig. 3a). These trajectories were normalized relative to the percentage of the path length traversed by the hand (instead of time) and averaged over five repetitions.

## III. RESULTS

We perform statistical tests to study whether our features are able to distinguish the behavior changes of the paretic/non-paretic arms in unimanual/bimanual modes, and to measure the inter-arm coupling strength at different joints. Fig. 4 shows representative mapping plots for Mapping 1-4. Statistical tests further compare the distribution of

the features among the joint angles, and between unimanual/bimanual modes, in two comparisons (see Fig. 3b).

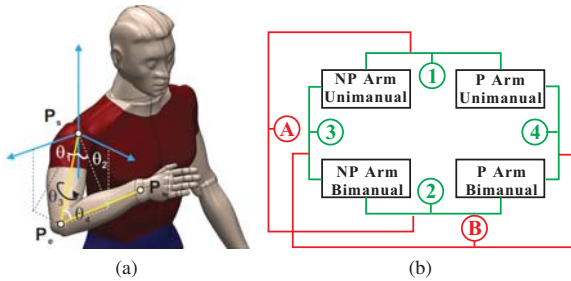


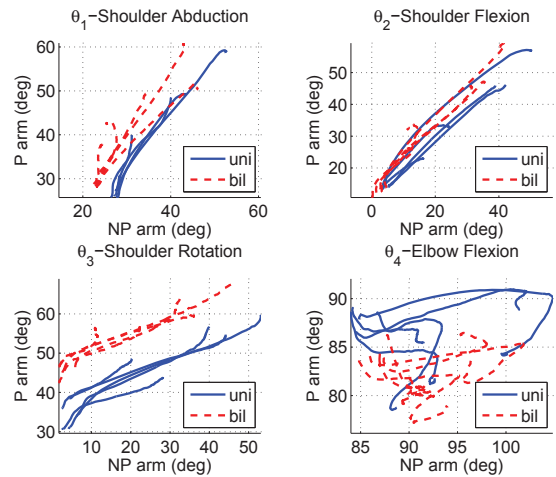
Fig. 3: (a) The four joint angles extracted from the reaching motions are the shoulder abduction ( $\theta_1$ ), shoulder flexion ( $\theta_2$ ), shoulder rotation ( $\theta_3$ ) and elbow flexion ( $\theta_4$ ). (b) Mapping symmetry and complexity features are extracted from the motion mappings of non-paretic (NP) arm and paretic (P) arm, denoted by numbers, for further comparisons denoted by letters.

Two-way ANOVA are used to compare among joints and between unimanual/bimanual modes. With 95% confidence level, significant differences are found among different joints in all the four mapping features, regardless of the motion modes and motor function of the arms, which are further investigated in the multiple comparison shown in Fig. 5. Only a few significant differences were found between motion modes (in Comparison A) and between non-paretic and paretic arms (in Comparison B), presented in Fig. 5e to 5h.

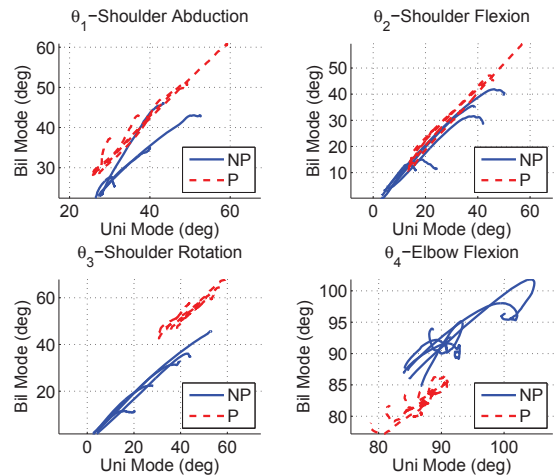
#### IV. DISCUSSION

##### A. Effect of Inter-arm Coupling on Arm Motion Symmetry

In both unimanual and bimanual modes, shoulder flexion  $\theta_2$  is the most symmetric joint. As shown in Fig. 5a and 5b, it has closest to ideal  $p_1$  and  $p_2$ , significantly highest  $R^2$  and lowest  $N_c$ . On the other hand, at both shoulder rotation  $\theta_3$  and elbow flexion  $\theta_4$ , the paretic arm traverses less of the joint space ( $p_1 < 1$ ) and has higher average arm posture (large positive  $p_2$ ) than the non-paretic arm. Shoulder abduction  $\theta_1$  is comparable to shoulder flexion  $\theta_2$  for its  $p_1$  and  $p_2$ , yet its  $R^2$  and  $N_c$  are as bad as shoulder rotation  $\theta_3$  and elbow flexion  $\theta_4$ . Comparison A further reveals that the symmetry at the shoulder flexion  $\theta_2$  is improved when both arms move together. In Fig. 5e,  $p_2$  is increased at  $\theta_2$ , while its mean is close to zero, which means that in unimanual mode, the paretic arm has lower average arm posture than the non-paretic arm, while in bimanual mode, the two arms have about the same posture. Such results imply that **the effect of inter-arm coupling depends on the task relevance of joints**. The task of reaching forward to touch the targets demands more motion at the shoulder flexion  $\theta_2$ , while the shoulder abduction  $\theta_1$  and rotation  $\theta_3$  are less task-relevant. Human motor control generally emphasizes the control of task-relevant joints, while loosely monitoring task-irrelevant joints [22]–[24]. Consistent with this general strategy of human motor control, inter-arm coupling imposes stronger motion synchronization effort at task-relevant joints.



(a) From non-paretic arm to paretic arm.



(b) From unimanual mode to bimanual mode.

Fig. 4: Representative mapping plots from a stroke subject. Given the mappings illustrated in Fig. 3b, in (a), blue solid lines refer to Mapping 1, while red dotted lines refer to Mapping 2; in (b), Blue solid lines refer to Mapping 3, while red dotted lines refer to Mapping 4.

##### B. Effect of Inter-arm Coupling on Arm Behavior Change

The inter-mode behavior changes of the paretic and non-paretic arms are shown in the multiple comparison among the joints in Fig. 5c and 5d. Shoulder flexion  $\theta_2$  is outstanding for highest  $R^2$  and lowest  $N_c$  for both arms. Comparison B found significant differences between the paretic and non-paretic arms: at  $\theta_2$ , the paretic arm traverses about the same distance in joint space ( $p_1$  is about 1) and maintains about the same average arm posture ( $p_2$  is about zero) for different modes, while the non-paretic arm traverses more of the joint space ( $p_1$  is about 1.1) and reduces the average arm posture ( $p_2 < 0$ ) in bimanual mode (see Fig. 5f to 5g). This indicates **the non-paretic arm contributes more to the improved motion symmetry in bimanual mode**.

Note that the paretic arm has higher posture in bimanual mode than in unimanual mode at the shoulder rotation  $\theta_3$  and elbow flexion  $\theta_4$  (see Fig. 5d for  $p_2$ ), which indicates that

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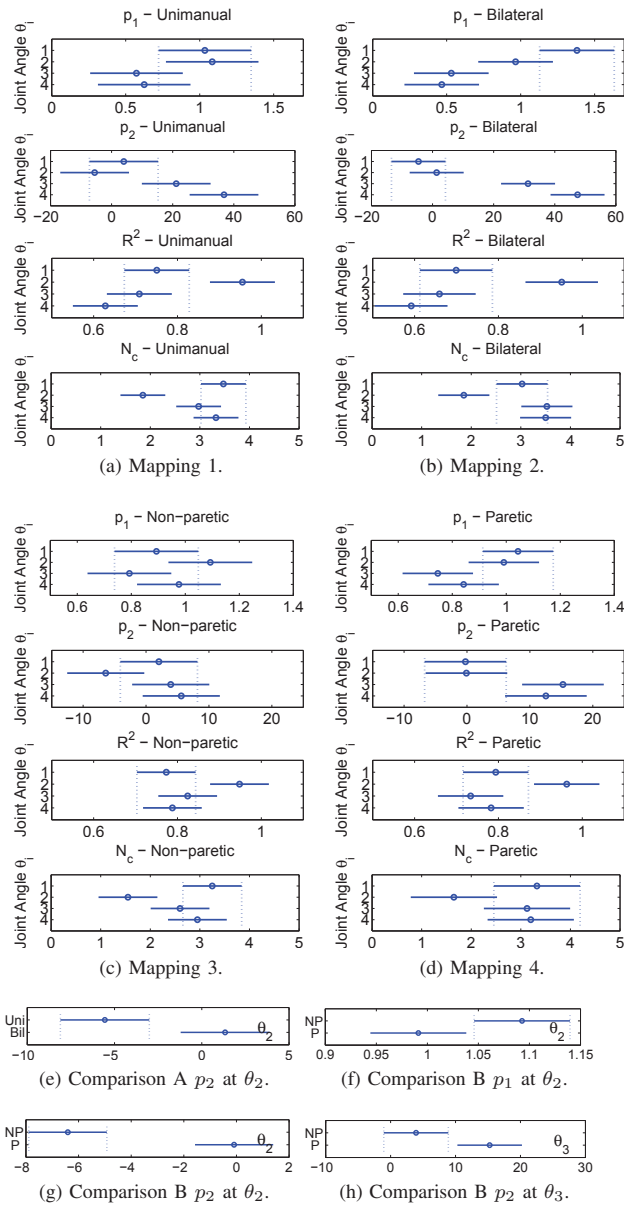


Fig. 5: Results of multi-comparison among joints (a-d). For comparisons between inter-arm mappings (Comparison A) and intern-mode mappings (Comparison B), only significant differences are displayed (e-h).

inter-arm coupling is changing the behavior of the paretic arm. Comparison B further shows that at  $\theta_3$ , the increase of arm posture is significantly more pronounced in the paretic arm than the non-paretic arm (see Fig. 5h). At the same time, at the shoulder flexion  $\theta_2$ , the paretic arm maintains its posture in bimanual mode, while the non-paretic arm significantly reduces its posture (see Fig. 5g). Such results suggest that **inter-arm coupling affect the behavior of both arms differently**: the paretic arm suppresses the shoulder flexion the non-paretic arm, while the non-paretic arm encourages the shoulder rotation of the paretic arm, both of which result in synchronization of motion tendency.

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